

FIG. 1. (Color online). The density functional calculated allowed chemical potential ranges (sum of all the colored parts

$$2\Delta\mu_{\rm Al} + \Delta\mu_{\rm Cu} \leq \Delta H_f({\rm Al}_2{\rm Cu}).$$
(8)

As shown in Fig. 1, $CuAlS_2$ is unstable with respect to formation of Al_2S_3 in the upper white area of Fig. 1, i.e., under Al-rich condition, (AlS, AlCu, and Al_2Cu pose weaker constrains, and are included in the Al_2S_3 ranges in Fig. 1). CuAlS₂ is also unstable with respect to CuS or Cu₂S precipi-



FIG. 2. The formation energy ΔH vs Fermi level for CuAlS₂:Mn, CuGaS₂:Mn, CuInS₂:Mn, CuGaSe₂:Mn, and CuGaTe₂:Mn with the chemical potentials at point *M* and *N* in Fig. 1. Mn prefers to III sites at point M, independent of E_F , while it prefers the Cu site at point N only in the shaded E_F ranges. For CuGaTe₂:Mn, Mn on Cu is unstable for all E_F

IV. SITE PREFERENCE OF Mn IN CHALCOPYRITES

Having calculated the chemical potential domains for $CuAlS_2$, $CuGaS_2$, $CuInS_2$, and $CuGaSe_2$ (Fig. 1), we next discuss the site preference of Mn in these chalcopyrites. The formation enthalpy for Mn substituting either the Cu or the III sites at different charge state are calculated using a single Mn atom in a 64 atom supercell according to^{16,17}

$$\Delta H_f^{(\alpha,q)} = E(\alpha,q) - E(0) + \sum_{\alpha} n_{\alpha} (\Delta \mu_{\alpha} + \mu_{\alpha}^{\text{Solid}})$$
$$+ q(E_{VBM} + E_F), \qquad (12)$$

where $E(\alpha,q)$ and E(0) are the total energy of the supercell with and without defect α . Here $(\Delta \mu_{\alpha} + \mu_{\alpha}^{\text{Solid}})$ is the absolute value of the chemical potential of atom α . Also n_{α} is the number of atoms for each defect; $n_{\alpha} = -1$ if an atom is added, while $n_{\alpha} = 1$ if an atom is removed. E_{VBM} represents the energy of the VBM of the defect-free system (which we take from the averaged eigenvalue of special k points) and E_F is the Fermi energy relative to the E_{VBM} . The atomic structure was fully relaxed in our calculation. The relaxation energy due to Mn substitution was 20–100 meV. The total energy of charged defects in a supercell calculation includes an error due to image charge interaction from periodic boundary condition. We therefore correct $E(\alpha,q)$ up to quadrupole term according to the Makov-Payne scheme.¹⁸ The correction raised $E(\alpha,q)$ by 120 to 300 meV for both q=1 and q=-1 charge states.

The functional relations between the formation energy and chemical potentials and E_F at different charge states are listed in Table II. The site preference of Mn is determined by

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- 27 Using the same structure of Ga₂Se₃, see Ref. 28.
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